
sect

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Azat Ibrakov

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Note: If object is not listed in documentation it should be considered as implementation detail that can change and should not be relied upon.

DECOMPOSITION MODULE

```
class sect.decomposition.Graph(root: Node)
```

Represents trapezoidal decomposition graph.

```
classmethod from_multisegment(multisegment: ~ground.hints.Multisegment, *, shuffler:
    ~typing.Callable[[~typing.MutableSequence], None] = <bound
    method Random.shuffle of <random.Random object>>, context:
    ~ground.base.Context) → Graph
```

Constructs trapezoidal decomposition graph of given multisegment.

Based on incremental randomized algorithm by R. Seidel.

Time complexity:

$O(\text{segments_count} * \log \text{segments_count})$ expected, $O(\text{segments_count} ** 2)$ worst

Memory complexity:

$O(\text{segments_count})$

where `segments_count = len(multisegment.segments)`

Reference:

<https://doi.org/10.1016%2F0925-7721%2891%2990012-4> <https://www.cs.princeton.edu/courses/archive/fall05/cos528/handouts/A%20Simple%20and%20fast.pdf>

Parameters

- **multisegment** – target multisegment.
- **shuffler** – function which mutates sequence by shuffling its elements, required for randomization.
- **context** – geometric context.

Returns

trapezoidal decomposition graph of the multisegment.

```
>>> from ground.base import get_context
>>> context = get_context()
>>> Multisegment, Point, Segment = (context.multisegment_cls,
...                                 context.point_cls,
...                                 context.segment_cls)
>>> graph = Graph.from_multisegment(
...     Multisegment([Segment(Point(0, 0), Point(1, 0)),
...                     Segment(Point(0, 0), Point(0, 1))]),
...     context=context
```

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```

... )
>>> Point(1, 0) in graph
True
>>> Point(0, 1) in graph
True
>>> Point(1, 1) in graph
False
>>> graph.locate(Point(1, 0)) is Location.BOUNDARY
True
>>> graph.locate(Point(0, 1)) is Location.BOUNDARY
True
>>> graph.locate(Point(1, 1)) is Location.EXTERIOR
True

```

classmethod from_polygon(*polygon*: ~ground.hints.Polygon, *, *shuffler*: ~typing.Callable[[~typing.MutableSequence], None] = <bound method Random.shuffle of <random.Random object>>, *context*: ~ground.base.Context) → *Graph*

Constructs trapezoidal decomposition graph of given polygon.

Based on incremental randomized algorithm by R. Seidel.

Time complexity:

$O(\text{vertices_count} * \log \text{vertices_count})$ expected, $O(\text{vertices_count} ** 2)$ worst

Memory complexity:

$O(\text{vertices_count})$

where

```

vertices_count = (len(polygon.border.vertices)
                  + sum(len(hole.vertices)
                        for hole in polygon.holes)
                  + len(extra_points) + len(extra_constraints))

```

Reference:

<https://doi.org/10.1016%2F0925-7721%2891%2990012-4> <https://www.cs.princeton.edu/courses/archive/fall05/cos528/handouts/A%20Simple%20and%20fast.pdf>

Parameters

- **polygon** – target polygon.
- **shuffler** – function which mutates sequence by shuffling its elements, required for randomization.
- **context** – geometric context.

Returns

trapezoidal decomposition graph of the border and holes.

```

>>> from ground.base import get_context
>>> context = get_context()
>>> Contour, Point, Polygon = (context.contour_cls, context.point_cls,
...                             context.polygon_cls)

```

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```

>>> graph = Graph.from_polygon(
...     Polygon(Contour([Point(0, 0), Point(6, 0), Point(6, 6),
...                        Point(0, 6)]),
...             [Contour([Point(2, 2), Point(2, 4), Point(4, 4),
...                        Point(4, 2)])]),
...     context=context
... )
>>> Point(1, 1) in graph
True
>>> Point(2, 2) in graph
True
>>> Point(3, 3) in graph
False
>>> graph.locate(Point(1, 1)) is Location.INTERIOR
True
>>> graph.locate(Point(2, 2)) is Location.BOUNDARY
True
>>> graph.locate(Point(3, 3)) is Location.EXTERIOR
True

```

property height: `int`

Returns height of the root node.

locate(*point: Point*) → `Location`

Finds location of point relative to decomposed geometry.

Time complexity:

$O(\text{self.height})$

Memory complexity:

$O(1)$

TRIANGULATION MODULE

```
class sect.triangulation.QuadEdge(start: Optional[Point] = None, left_from_start: Optional[QuadEdge] =  
None, rotated: Optional[QuadEdge] = None, *, context: Context)
```

Based on:

quad-edge data structure.

Reference:

<https://en.wikipedia.org/wiki/Quad-edge> http://www.sccg.sk/~samuelcik/dgs/quad_edge.pdf

```
classmethod from_endpoints(start: Point, end: Point, *, context: Context) → QuadEdge
```

Creates new edge from endpoints.

property end: Point

aka “Dest” in L. Guibas and J. Stolfi notation.

property left_from_end: QuadEdge

aka “Lnext” in L. Guibas and J. Stolfi notation.

property left_from_start: QuadEdge

aka “Onext” in L. Guibas and J. Stolfi notation.

property opposite: QuadEdge

aka “Sym” in L. Guibas and J. Stolfi notation.

property right_from_end: QuadEdge

aka “Rprev” in L. Guibas and J. Stolfi notation.

property right_from_start: QuadEdge

aka “Oprev” in L. Guibas and J. Stolfi notation.

property rotated: QuadEdge

aka “Rot” in L. Guibas and J. Stolfi notation.

property start: Point

aka “Org” in L. Guibas and J. Stolfi notation.

```
connect(other: QuadEdge) → QuadEdge
```

Connects the edge with the other.

```
delete() → None
```

Deletes the edge.

```
orientation_of(point: Point) → Orientation
```

Returns orientation of the point relative to the edge.

splice(*other*: QuadEdge) → None

Splices the edge with the other.

swap() → None

Swaps diagonal in a quadrilateral formed by triangles in both clockwise and counterclockwise order around the start.

class sect.triangulation.Triangulation(*left_side*: QuadEdge, *right_side*: QuadEdge, *context*: Context)

Represents triangulation.

classmethod constrained_delaunay(*polygon*: Polygon, *, *extra_constraints*: Sequence[Segment] = (),
extra_points: Sequence[Point] = (), *context*: Context) →
Triangulation

Constructs constrained Delaunay triangulation of given polygon (with potentially extra points and constraints).

Based on

- divide-and-conquer algorithm by L. Guibas & J. Stolfi for generating Delaunay triangulation,
- algorithm by S. W. Sloan for adding constraints to Delaunay triangulation,
- clipping algorithm by F. Martinez et al. for deleting in-hole triangles.

Time complexity:

$O(\text{vertices_count} * \log \text{vertices_count})$ for convex polygons without extra constraints,
 $O(\text{vertices_count} ** 2)$ otherwise

Memory complexity:

$O(\text{vertices_count})$

where

```
vertices_count = (len(polygon.border.vertices)
                  + sum(len(hole.vertices)
                        for hole in polygon.holes)
                  + len(extra_points) + len(extra_constraints))
```

Reference:

http://www.sccg.sk/~samuelcik/dgs/quad_edge.pdf https://www.newcastle.edu.au/__data/assets/pdf_file/0019/22519/23_A-fast-algorithm-for-generating-constrained-Delaunay-triangulations.pdf
<https://doi.org/10.1016/j.advengsoft.2013.04.004> http://www4.ujaen.es/~fmartin/bool_op.html

Parameters

- **polygon** – target polygon.
- **extra_points** – additional points to be presented in the triangulation.
- **extra_constraints** – additional constraints to be presented in the triangulation.
- **context** – geometric context.

Returns

triangulation of the border, holes & extra points considering constraints.

classmethod delaunay(*points*: Sequence[Point], *, *context*: Context) → *Triangulation*

Constructs Delaunay triangulation of given points.

Based on divide-and-conquer algorithm by L. Guibas & J. Stolfi.

Time complexity:

$O(\text{len}(\text{points}) * \log \text{len}(\text{points}))$

Memory complexity:

$O(\text{len}(\text{points}))$

Reference:

http://www.sccg.sk/~samuelcik/dgs/quad_edge.pdf

Parameters

- **points** – 3 or more points to triangulate.
- **context** – geometric context.

Returns

triangulation of the points.

delete(*edge*: QuadEdge) → None

Deletes given edge from the triangulation.

triangles() → List[Contour]

Returns triangles of the triangulation.

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